Piezoelectric Transducer Apparatus Having
Independent Gain and Phase Characteristics Functions

Field of the Invention

5   This invention relates in general to piezoelectric transducers and, in particular, to a piezoelectric transducer apparatus having independent gain and phase characteristic functions.

Background of the Invention

10   Piezoelectricity is a phenomenon in which positive and negative electric charges appear on opposite sides of some non-conducting crystals when subjected to mechanical pressure. The converse piezoelectric effect, electrostriction, is the property of some non-conductors, or dielectrics, that deform slightly under the application of an electric field. Piezoelectricity and electrostriction are the

15   reciprocating conversions of mechanical and electrical energy back and forth by piezoelectric workpieces that can be utilized in various applications such as vibration detection and actuation of controlled structures.

Traditional piezoelectric point sensors are used primarily for the detection and measurement of vibrations on a specific point on an examined structure. Shape

20   and type of these piezoelectric sensors can be modified in order to meet the need for the detection of, for example, the vibration of an examined structure in the axial direction. Such sensors are easily customizable to various structural configurations and have been widely utilized in many applications.

However, these prior-art piezoelectric point sensors have a basic characteristic

25   that limits their application. Frequency response characteristics of these point sensors are self-constrained by characteristics of their own structural configuration. For example, traditional point sensors are limited in their useful frequency response ranges due to their structural configuration characteristics. Electronic circuitries have to be employed based on the traditional filter theory.

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However, sensor frequency response characteristics are thus altered such that their usefulness jeopardized.

Further, these prior-art piezoelectric point sensors can only be useful for the detection of the structural characteristics of single points on an examined structure.

5   One single point sensor does not reveal the structural characteristics of an examined target in their entirety. When the scope of sense and detection for a target structure needs to be large, excessive number of point sensors have to be installed. The resulted vast amount of information collected by these sensors present processing problems for the detection system. As a result, utilization of

10   large numbers of these point sensors in applications such as real time control of a structure becomes complicated and unrealistic.

On the other hand, since the emergence of distributed sensor theories in the 1980s, it has become clear that useful bandwidth of piezoelectric sensors can be designed and controlled flexibly to an extent. This is possible by control and

15   adjustment in parameters such as shape and polarization direction of the electrode of a distributed sensor. Due to the fact that the electrode of a distributed sensor is distributed continuously over an extent in space, it is therefore possible for a distributed sensor to measure the overall structural vibration information of an examined target structure. Measurement of force distribution in the structure in

20   the sensed extent is also possible. However, since different distributed sensor configurations have to be implemented costly for the measurement of different target structures, the design and construction efforts in these distributed sensors therefore limit their application.

Based on traditional piezoelectricity theories, gain and phase characteristics

25   for electrical signals detected in piezoelectric devices, either those for mechanical vibration sensing or those for electrical signal filtering, are inter-dependent. The inter-relationship between the gain and phase characteristics for piezoelectric devices that has been difficult to control have placed limitations to their design.

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Summary of the Invention

It is therefore an object of the present invention to provide a piezoelectric transducer apparatus having independent gain and phase characteristic functions.

The present invention achieves the above and other objects by a piezoelectric transducer apparatus that comprises at least one piezoelectric unit and a body structure. Each of the at least one piezoelectric unit has a piezoelectric block and at least one pair of electrodes. Each electrode is adhered to one surface of the piezoelectric block. Each of the at least one piezoelectric unit is adhered to the surface of the body structure with the electrode exposed externally. The electrode shape of the electrode of each of the at least one piezoelectric unit is matched to a desired body strain pattern existing in the body structure wherein the electrode of each of the at least one piezoelectric unit may excite a strain pattern in the body structure that is the same as the desired body strain pattern. The body structure of any structural configuration may have a resolved electrode shape that achieves disengagement of the phase and gain characteristics of the piezoelectric construction based on that particular body structure.

Brief Description of the Drawings

Figures 1A and 1B respectively show the gain and phase characteristics as functions of frequency for a piezoelectric sensor construction having incorporated spatial filter;

Figures 2A and 2B respectively show the gain and phase characteristics as functions of frequency for a piezoelectric sensor construction having incorporated modal sensor;

Figures 3A and 3B outline the angle of about 45 degrees formed between the principal axes of the material characteristic orientation and of the structural configuration of a piezoelectric sensor workpiece;

Figure 4 is an exploded perspective view of a piezoelectric transducer apparatus in accordance with an embodiment of the present invention

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schematically showing the basic structural configuration thereof;

Figure 5 is a perspective view outlining the selection of the target origin in an embodiment of the inventive piezoelectric transducer apparatus utilized as a vibration detector;

5   Figure 6 is a perspective view illustrating the selection of the target origin at the free end of an embodiment of the inventive piezoelectric transducer apparatus utilized as a spatial filter;

Figure 7 shows the characteristic curve of the apparatus of Figure 6 in the infinite domain that exhibits the characteristics of an even function;

10   Figure 8 is a perspective view illustrating an embodiment of the inventive piezoelectric transducer apparatus utilized as a spatial filter having the target origin selected at the fixed end that exhibits the characteristics of an odd function;

Figure 9 shows the characteristic curve of the apparatus of Figure 7 in the infinite domain that exhibits the characteristics of an odd function;

15   Figure 10 shows the characteristic curve of an embodiment of the inventive piezoelectric transducer apparatus utilized as a spatial filter in the infinite domain and having the target origin selected at the fixed end;

Figure 11 shows the characteristic curve of an embodiment of the inventive piezoelectric transducer apparatus utilized as a spatial filter in the infinite domain and having the target origin selected at the free end;

20   Figure 12 shows the gain characteristics as a function of frequency for a band-pass filter constructed by the superposition of discrete spatial filters;

Figures 13A and 13B respectively show the gain and phase characteristics as functions of frequency for a band-pass filter that exhibit increased effective

25   frequency range;

Figure 14 schematically illustrates the superposition of discrete spatial filters involving no change in the direction of polarization for the design of the inventive piezoelectric transducer apparatus;

Figures 15A and 15B schematically illustrate the use of the method of

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imaging in the expansion of a sine function onto the infinite domain in the design of an inventive piezoelectric transducer apparatus based on a fixe-free cylindrical body structure;

Figures 16A and 16B schematically illustrate the use of the method of imaging in the expansion of a sine function onto the infinite domain in the design of an inventive piezoelectric transducer apparatus based on a free-free cylindrical body structure;

Figures 17A and 17B schematically illustrate the use of the method of imaging in the expansion of a sine function onto the infinite domain in the design of an inventive piezoelectric transducer apparatus based on a fixed-fixed cylindrical body structure;

Figure 18 is a perspective view illustrating an embodiment of a spatial filter based on the inventive piezoelectric sensor apparatus having a fixed-free cylindrical body structure;

Figures 19A and 19B respectively show the gain and phase characteristics as functions of frequency for an embodiment of a band-pass filter based on the inventive piezoelectric sensor apparatus having a fixed-free cylindrical body structure;

Figure 20 is a perspective view illustrating an embodiment of a high-pass filter based on the inventive piezoelectric sensor apparatus having a fixed-free cylindrical body structure;

Figures 21A and 21B respectively show the gain and phase characteristics as functions of frequency for an embodiment of a high-pass filter based on the inventive piezoelectric sensor apparatus having a fixed-free cylindrical body structure;

Figure 22 is a perspective view illustrating the electrode design of an asymmetric effective surface having a target origin that is neither located at the body structural center nor at the body structural boundary;

Figure 23 is a perspective view illustrating another electrode design of an

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asymmetric effective surface having a target origin that is neither located at the body structural center nor at the body structural boundary;

Figure 24 is a perspective view illustrating the asymmetric effective surface electrode of an embodiment of the inventive piezoelectric transducer apparatus designed by the superposition of discrete effective surface electrodes, with the fixed-free cylindrical body structure;

Figure 25 is a perspective view illustrating another asymmetric effective surface electrode of an embodiment of the inventive piezoelectric transducer apparatus designed by the superposition of discrete effective surface electrodes, with the target origin biased toward the free end of the fixed-free cylindrical body structure;

Figure 26 is a perspective view illustrating yet another asymmetric effective surface electrode of an embodiment of the inventive piezoelectric transducer apparatus designed by the superposition of discrete effective surface electrodes, with the target origin biased toward the free end of the fixed-free cylindrical body structure;

Figure 27 is a perspective view illustrating the asymmetric effective surface electrode of an embodiment of the inventive piezoelectric transducer apparatus designed by the superposition of discrete effective surface electrodes, with the target origin biased toward the fixed end of the fixed-free cylindrical body structure;

Figure 28 is a perspective view illustrating another asymmetric effective surface electrode of an embodiment of the inventive piezoelectric transducer apparatus designed by the superposition of discrete effective surface electrodes, with the target origin biased toward the fixed end of the fixed-free cylindrical body structure;

Figure 29 is a perspective view illustrating yet another asymmetric effective surface electrode of an embodiment of the inventive piezoelectric transducer apparatus designed by the superposition of discrete effective surface electrodes,

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with the target origin biased toward the fixed end of the fixed-free cylindrical body structure;

Figure 30 is a perspective view illustrating still another asymmetric effective surface electrode of an embodiment of the inventive piezoelectric transducer apparatus designed by the superposition of discrete effective surface electrodes, with the target origin biased toward the fixed end of the fixed-free cylindrical body structure;

Figure 31 is a perspective view illustrating an embodiment of the inventive piezoelectric sensor apparatus having the boundary condition set neither to the fixed nor to the free end;

Figure 32 is a schematic diagram illustrating the application of an embodiment of the inventive piezoelectric transducer apparatus in an inspection and test device by integrating with an interface circuit and featuring a suitably-selected effective surface electrode;

Figure 33 illustrates the characteristics of the device of Figure 32 in the complex plane;

Figure 34 is a block diagram illustrating the basic circuit configuration of a sense and control device having an active sensor feedback loop based on either the expansion or the compression effect of the piezoelectric body structure;

Figure 35 is a block diagram illustrating the basic circuit configuration of another sense and control device having an active sensor feedback loop based on the torsional effect of the piezoelectric body structure; and

Figure 36 illustrates the characteristics curve of an active inspection and test device in the infinite domain.

Detailed Description of the Invention

Figures 1A and 1B respectively show the gain and phase characteristics as functions of frequency for a piezoelectric sensor construction having incorporated the concept of a spatial filter. In the gain characteristics of Figure 1A, a sensor

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with a conventional sensor structural configuration has a gain characteristics represented by the curve 11, which has a useful bandwidth within the frequency range generally represented by reference numeral 14. By contrast, another sensor incorporating the design concept of a spatial filter into its structural configuration

5   has the gain characteristics 12, with a useful bandwidth 15. This gain characteristics 12 is the result of incorporation of the characteristics 13 of a spatial filter into the characteristics 11 of the plain sensor. As is illustrated, the useful bandwidth 15 achieved by the sensor incorporating the spatial filter concept (having the characteristics 12) is substantially larger than 14 of the other (11).

10   Meanwhile, in the phase characteristics of Figure 1B, characteristics curves 16 and 17 represent the phase characteristics of the sensors described in Figures 1A and 1B having and having not incorporated the concept of a spatial filter respectively. The substantially flat characteristic shown by curve 16 indicates that the phase characteristics of the sensor incorporating the spatial filter concept is

15   able to be disengaged from the its own gain characteristics. How this is possible and achieved are described in the following paragraphs.

Figures 2A and 2B respectively show the gain and phase characteristics as functions of frequency for a piezoelectric sensor construction having incorporated the concept of a modal sensor. In the gain characteristics of Figure 2A, a sensor

20   with a conventional point sensor structural configuration has a gain characteristics represented by the curve 21, which has a useful bandwidth within the frequency range 24. Note that in the frequency range of the depicted gain characteristic, the conventional point sensor has first and second modes of gain peaks included.

By contrast, another sensor incorporating the design concept of a modal

25   sensor into its structural configuration has the gain characteristics 22, with a useful bandwidth 25. The useful bandwidth 25 achieved by the sensor incorporating the modal sensor concept is larger than 24 of the other as the first mode in the point sensor has been expelled. Only second mode is present. Similar as in the case of Figure 1A, gain characteristics 22 is the result of incorporation of the

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characteristics of a modal sensor into the characteristics 21 of a plain point sensor.

On the other hand, in the phase characteristics of Figure 2B, characteristics curves 26 and 27 represent the phase characteristics of the sensors described in Figures 2A and 2B having and having not incorporated the concept of a modal sensor respectively. The substantially flat characteristic extending into the high end of the frequency scale shown by curve 26 indicates that the phase characteristics of the sensor incorporating the modal sensor concept is able to be disengaged from its own gain characteristics. Again, details of this achievement is described in the following paragraphs. Note, in Figure 2B, that the flat line 28 identifies a constant phase angle that assist to demonstrate the substantial linearity of the characteristics curve 26 up to the high end of the frequency scale.

It should be noted that each of both the methodologies of modal expansion and characteristic polynomial expansion can be employed to implement adjustment on the mathematical gain function of the structural system of the body construction of a piezoelectric sensor apparatus. It is possible to achieve phase adjustment without following the principles of a causal system as in the theory of traditional electronic filter circuits. One of the specially devised exception to the principle of causal systems is a sensor system in which the system gain expressed as a function of frequency can be effectively adjusted without incurring a corresponding shifts in its phase. Details are described below.

In the following description of inventive piezoelectric transducer apparatus, including how the disengagement between the gain and phase characteristics in the apparatus can be achieved, a particular type of second-order body structure for the construction of the apparatus is used as an example of the mathematical development. In general, a piezoelectric transducer apparatus of the present invention comprises a number of piezoelectric sensor units adhered to the surface of the sensor body structure, as will be described in detail with reference to Figure 3 of the drawing.

The description that the body structure used for the construction of the

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inventive piezoelectric transducer apparatus is second order is referring to the fact that the constitutive equation for the apparatus is second order equation. Note, however, that although second order structural systems are utilized herein for the description of the present invention, it is not the intention of this description to limit the scope of the present invention to apparatuses having second order constructions. Rather, the underlying principle of the present invention indicates that a body structure of any structural configuration may have a resolved electrode shape that achieves disengagement of the phase and gain characteristics of the piezoelectric construction based on that particular body structure.

A mathematical modeling and analysis methodology will be described in the following paragraphs that can be employed for determining the electrode shape matched to the three-dimensional body strain pattern existing in a body structure of any shape. In a piezoelectric construction having a matched electrode, the body strain pattern existing in the body structure of the piezoelectric construction matches the strain pattern if excitation is provided by the matched electrode.

The governing equations of a thin-plate piezoelectric workpiece is described in the following paragraphs.

Based on the first law of thermodynamics, the constitutive equations for the piezoelectric workpiece can be expressed as:

$$T_p = c_{pq}^E S_q - e_{kp} E_k \qquad (1)$$

$$D_i = e_{iq} S_q + \in_{ik}^s E_k , \qquad (2)$$

or

$$S_P = s_{pq}^E T_q + d_{kp} E_k \qquad (3)$$

$$D_i = d_{iq} T_q + \in_{ik}^T E_k , \qquad (4)$$

wherein $i, j, k = 1\text{-}3$, $p, q = 1\text{-}6$, T_p and S_q are stress and strain respectively, E_k is the electric field intensity, D_i is the electric displacement and c_{pq}, $\in_{ij}$, $s_{pq} = (c_{pq})^{-1}$, e_{kp} and d_{ip} are, respectively, the elastic stiffness matrix, the permittivity matrix, the elastic compliance matrix, the piezoelectric stress matrix and the piezoelectric

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strain matrix, as defined in the IEEE Compact Matrix Notation system. The notation system was published in 1987 by IEEE in the *IEEE Standard on Piezoelectricity*.

The signal measured over the surface of the electrode of a piezoelectric workpiece can be determined employing Gauss' theorem:

$$q(t) = \int_{\underline{S}} \underline{D} \cdot d\underline{\sigma} . \tag{5}$$

Piezoelectric sensor equation can be obtained by considering the inter-relationship between strain and stress of the sensor units attached to the body structure of the system, utilizing the governing equations for piezoelectricity. Thus, the sensor equation for the thin piezoelectric workpieces utilized as the sensor units can be expressed as:

$$q(t) = \iint_{S^{(12)}} \left[e_{31} \frac{\partial u}{\partial x} + e_{32} \frac{\partial v}{\partial y} + e_{36} \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right) \right] dxdy \\ - z^0 \iint_{S^{(12)}} \left[e_{31} \frac{\partial^2 w}{\partial x^2} + e_{32} \frac{\partial^2 w}{\partial y^2} + 2 e_{36} \frac{\partial^2 w}{\partial xy} \right] dxdy \tag{6}$$

In equation (6), u and v in the first integral part to the right of the equal sign are the displacements in the x and y directions of the system respectively, which represent the response presented by the system due to the in-plane strain. On the other hand, w in the second integral part in the equation is a measure of the bending displacement of the system, which represents the response presented by the system due to the out-of-plane strain.

Figures 3A and 3B outline the angle of about 45 degrees formed between the principal axes of the material characteristic orientation and of the structural configuration of a piezoelectric sensor workpiece. In Figure 3A the direction parallel to the X1 axis represents the principle axis of the material characteristic orientation, as determined by the crystals in the material block of the piezoelectric workpiece in question. Rectangles 32 and 33 represents blocks of piezoelectric workpieces that can be cut from the material block. Longitudinal axes of

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Rectangles 32 and 33 are arranged to be swung away from the principle axis of material characteristic orientation for about 45 degrees in both directions. Workpieces thus obtained, namely blocks represented by rectangles 32 and 33 in Figure 3A, may be integrated together for the construction of a piezoelectric sensor unit 34 shown in the perspective view of Figure 3B. A piezoelectric sensor unit 34 thus constructed may be equipped with polarization directions perfectly suitable for consideration in the above sensor equation.

Figure 4 is an exploded view of a piezoelectric transducer apparatus in accordance with an embodiment of the present invention. The illustration schematically shows the basic structural configuration of a typical piezoelectric transducer apparatus that can be modeled mathematically as a second order system. In the drawing, the apparatus is shown to comprise a sensor body structure 41, and four piezoelectric sensor units 42, 43, 44 and 45. More or less than four sensor units are possible depending on application.

Each of the piezoelectric sensor units is a piezoelectric workpiece comprising a block of piezoelectric material and at least a pair of surface electrodes. For example, the piezoelectric sensor unit 45 comprises a block of piezoelectric material 417 in the form of a two-dimensional thin plate, and a pair of electrodes 412 and 413 adhered to the opposite side surfaces.

All the surface electrodes for the piezoelectric sensor units, namely electrodes 46, 47, 48, 49, 410, 411, 412 and 413 shown in the drawing, may be prepared in shapes for adequate spatial distribution. Each of the surface electrodes with its designed shape can be selectively adhered to the surface of the block of piezoelectric material. Electric currents in the system, for example, currents arising from strain inside the piezoelectric block, can be collected via these electrodes and relayed to interface circuits connected to the piezoelectric apparatus. Electrodes in the illustrated apparatus such as 46, 49, 410 and 413 may also serve as ground electrodes to provide EMI shielding for the apparatus. Further, opposite remote ends of the piezoelectric sensor body structure 41

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identified by reference numerals 10 and 20 respectively may be selected to be the boundary for setting up the boundary condition in the mathematical analysis system of the apparatus.

For the convenience of the description of the present invention, a few types of body structure suitable for the construction of the inventive piezoelectric transducer apparatus that can be described and analyzed in second order mathematical modeling systems are examined here. They include elongated pieces of suitable material that can be approximated mathematically as one-dimensional body structures. As is comprehensible, this requires that the traverse dimension of these elongated body structures be virtually neglectable compared to the longitudinal dimension.

If the mechanical vibrations allowed in the analyzed system are constrained to pure compression and/or expansion in the direction of the longitudinal axis of the body structure, elongated rods of any cross-sectional shape are applicable. Note that the arbitrary shape refers to the shape taken by cutting the elongated body structure in a plane perpendicular to the longitudinal axis.

As another example, if the mechanical vibrations in the system are restricted to pure torsion in the body structure, elongated rods of circular cross section are applicable. Certainly, the diameter of the rods should be sufficiently small as compared to the length.

Mathematically, for a one-dimensional rod of any cross-sectional shape that vibrates in the longitudinal direction, the governing equation can be expressed as

$$E\frac{\partial^2 u(x,t)}{\partial x^2} + R\frac{\partial^3 u(x,t)}{\partial t \partial x^2} - \rho\frac{\partial^2 u(x,t)}{\partial t^2} = 0 \tag{7}$$

wherein E is the piezoelectric stiffness constant, is density, u is the displacement in the structural cross section, and x in the expression indicates that the traverse displacements is only concerned in the longitudinal direction of the system. Note that in the expression, the damping factor R of the system is taken into consideration.

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On the other hand, for a one-dimensional rod of circular cross-sectional shape that exhibits pure torsional vibrations, the governing equation is

$$G\frac{\partial^2 \theta(x,t)}{\partial x^2} + R\frac{\partial^3 \theta(x,t)}{\partial t \partial x^2} - \rho\frac{\partial^2 \theta(x,t)}{\partial t^2} = 0 \qquad (8)$$

wherein G is shear modulus, is density, is the twisting angle and, again, x in the expression indicates that the twisting angle is only concerned in the longitudinal direction of the system. Also, the damping consideration is also included in the analyzed system.

Mathematical solution to the above governing equations for the one-dimensional rods with either longitudinal or torsional vibrations can be obtained employing the technique of characteristic polynomial expansion. In the case of longitudinal vibration in the one-dimensional system, the characteristic polynomial expansion is implemented in terms of the longitudinal displacement of the sensor body structure by performing wave modes. The solution for the body strain, which is a function $u(x, t)$ of time t and the body structure physical dimension x, as obtained for the governing equation (7) can be expressed as

$$u(x,t) = [w_{lp}e^{jk_{lp}x} + w_{rp}e^{-jk_{rp}x}]e^{jwt} . \qquad (9)$$

In a similar manner, for the case of torsional vibration in the one-dimensional system, the characteristic polynomial expansion is implemented in terms of the torsional twists expressed as angular displacement of the sensor body structure by performing wave modes expansion. The solution for the body strain, which can be represented by an angular displacement function $\theta(x, t)$ of time t and the body structure physical dimension x, as obtained for the governing equation (8) can be expressed as

$$\theta(x,t) = [w_{lp}e^{jk_{lp}x} + w_{rp}e^{-jk_{rp}x}]e^{jwt} . \qquad (10)$$

Comparing solution equations (9) and (10), it can be noticed that both types elongated rods - with either longitudinal or torsional vibration - sustain substantially the same wave propagation characteristics. The only discrepancies

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being the type of vibration and their respective stiffness and shear modulus. In the solution equations, jk_{lp} and $-jk_{rp}$ are, respectively, the two imaginary roots in the frequency dispersion relationship, w_{lp} and w_{rp} are, respectively, the amplitudes of the propagating wave in the opposite directions. These two wave propagation

5   constants will be different depending on the selected different boundary conditions in the mathematical model of the sensor body structure. These two types of vibration in their respective one-dimensional rod-shaped body structures constitute the basis for the construction of very effective tools for the sensing and actuation of structures featuring disengaged phase and gain characteristics in the system.

10   Piezoelectric transducer apparatus in the form of both the one-dimensional elongated body structure described above, namely, the one-dimensional rod of longitudinal vibration and the one-dimensional shaft of torsional vibration can be described in a generalized sensor equation

$$q(k) = jk\Lambda \int_0^a \varsigma(x)[w_{lp}e^{jkx} - w_{rp}e^{-jkx}]dx \qquad (11)$$

15   wherein L is a product of both the piezoelectric strain constant and the surface integral. Note that this is assuming a second order system. Also note that $\varsigma(x)$ represents the effective surface electrode of the piezoelectric workpiece expressed as a function of the dimension x. $\varsigma(x)$ in the body structure of the system is a function of only one variable, the physical dimension of the body structure in the

20   longitudinal direction.

Effective surface electrode $\varsigma(x)$, being expressed as a function of the dimensional variable x, is a convenient means in the form of a mathematical equation for determining the geometrical shape of the substantial electrode of a piezoelectric sensor unit that is required for the construction of the inventive

25   piezoelectric transducer apparatus.

It can be found in the sensor equation (11) that regardless of either longitudinal or torsional vibration in the elongated rod-shaped body structure, a

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second order piezoelectric transducer apparatus of the present invention is capable of being constructed into a vibration detecting device that has disengaged phase and gain characteristics. Filtering effect can be provided by these devices for different types of structural vibration.

5   Essentially, the underlying concept of the present invention lies in the finding that in the finite body structure of a piezoelectric transducer apparatus, for any three-dimensional body strain pattern existing in the body structure, there exists a corresponding electrode having a specific shape, which, if used to excite the body structure by feeding electric energy into the body structure, generates the same

10   strain pattern. A mathematical modeling and analysis methodology is disclosed by the present invention that can be employed for determining the electrode shape matched to the three-dimensional body strain pattern existing in a body structure of any shape. A piezoelectric transducer apparatus equipped with the resolved electrode shape that matches the strain pattern has a phase characteristics that is

15   independent from the gain characteristics.

The piezoelectric transducer apparatus as described in Figure 4 which incorporates the structural configuration of the spatial filter is able to achieve independence between the gain and phase characteristics for the same piezoelectric system. Various methodologies can be translated into system design

20   parameters for the construction of a piezoelectric transducer apparatus of the present invention. These include facilitating, in the piezoelectric transducer apparatus being designed, the designation of the target origin, the employment of the concept of wave propagation, the selection of the base of the spatial filter, the superposition of the spatial characteristics of the piezoelectric material in the

25   system, the method of imaging, the selection of the integrated interfacing circuits, the manipulation of the boundary conditions in the mathematical system, the selection of the frequency-selective electrodes of the piezoelectric sensor unit, the application of the wave propagation theory, and the application of electronic circuit feedback schemes.

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The underlying concept for the design of spatial filters relies on the utilization of two-sided Laplace transform as the basic design tool. The only condition fulfilling the effectiveness of spatial filtering falls onto the origin 0 of the two-sided Laplace transform. This origin serves as the target origin for implementing

5   the design of the piezoelectric transducer apparatus of the present invention. Proper selection of this target origin in the system of the piezoelectric sensor construction (400 in Figure 4) facilitates optimized design results for various piezoelectric transducer apparatus featuring different effectiveness for different applications.

10   Figure 5 is a perspective view outlining the selection of the target origin in an embodiment of the inventive piezoelectric transducer apparatus utilized as a vibration detector. In the sensor construction 500 illustrated in the drawing for a piezoelectric transducer apparatus, the target origin 50 is set approximately to the center of the body structure 51 along the longitudinal axis x. The construction 500

15   has a free end 54 and a fixed end 53. As is comprehensible, the fixed end 53 of the body structure 51 is attached to a support base 55, and the free end 54 is left unsupported. Such a construction 500, equipped with an electrode 52 having the shape determined by the effective surface electrode $\varsigma(x)$, is suitable for use as a piezoelectric sensor device that maintains its fixed phase even though the gain in

20   the system is changed.

As the wave propagation in the body structure of a sensor construction reaches to the physical boundary, different scenarios of phase shift and/or energy consumption are possible as a result of different boundary conditions. Common boundary conditions are free and fixed boundaries. Fixed-free set of boundary

25   condition arrangement is typical for piezoelectric sensor constructions. The concept of imaging in the study of wave motion in elastic solids is helpful in the design of piezoelectric sensor constructions. The employment of imaging concept assists in transferring the discussion of the system between the infinite and the finite domains.

Figure 6 is a perspective view illustrating the selection of the target origin at the free end of an embodiment of the inventive piezoelectric transducer apparatus utilized as a spatial filter. In the construction 600 having the effective surface electrode 62, the target origin 60 is set to the free end 64 of the body structure 61.

5 In this construction, a spatial filter has a characteristics of an even function shown in Figure 7 as envisaged in the infinite domain. Figure 7 shows the characteristic curve of the apparatus of Figure 6 in the infinite domain that exhibits the characteristics of an even function.

Similarly, Figure 8 is a perspective view illustrating an embodiment of the

10 inventive piezoelectric transducer apparatus utilized as a spatial filter having the target origin selected at the fixed end that exhibits the characteristics of an odd function. A spatial filter envisaged in the infinite domain in this construction 800 has a characteristics of an odd function shown in Figure 9.

Thus, the concept of imaging can be employed to manipulate different

15 boundary condition arrangements in the design of the inventive piezoelectric transducer apparatus. The substantial body structure of a sensor construction in the finite domain may be transformed into the infinite domain for mathematical modeling and analysis. Wave propagation can be considered in the analysis as being in the infinite domain instead of the finite one of the real world. Figure 10

20 shows the characteristic curve of an embodiment of the inventive piezoelectric transducer apparatus utilized as a spatial filter in the infinite domain and having the target origin selected at the fixed end.

In Figure 10, the coarse section 101 represents an example of the wave propagation in the body structure, the entire fine section 102 extending in both the

25 positive and negative directions at the free end 40 and the fixed end 30 respectively, represents the finite domain in which the sensor body structure resides. Curve 103 correspondingly represents the characteristics of the construction in terms of wave propagation as envisaged in the infinite domain transformed from the finite domain 102 by applying imaging. The characteristics

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clearly shows itself as an odd-function characteristics in the infinite domain.

By contrast, Figure 11 shows the characteristic curve of an embodiment of the inventive piezoelectric transducer apparatus utilized as a spatial filter in the infinite domain and having the target origin selected at the free end.

5   Characteristics curve 113 identifies that the piezoelectric construction exhibits an even-function characteristics of a spatial filter having disengaged phase and gain characteristics.

As described, once the mathematical analysis of a finite domain piezoelectric construction is transformed into the infinite domain applying the technique of

10   either window functioning or the manipulation of boundary condition arrangements, Laplace transform becomes a valuable tool of design. Basic considerations in a spatial filter relates to wave propagation. In a piezoelectric construction based on a cylindrical body structure that conforms to a second order system, the mathematical expression for the effective surface electrode $\varsigma(x)$ in

15   terms of the dimensional variable x can be shown to be resolved into exponential functions.

Wave propagation in these constructions are expressed as exponential functions of the natural logarithmic base. Therefore, whenever an effective surface electrode for the sensor units of these constructions is contoured into a

20   shape conforming to a corresponding $\varsigma(x)$ incorporating the base of exponential functions, the characteristics of the spatial filter built out of the construction can be effectively controlled. In other words, surface electrodes shaped in accordance with different exponential bases can be utilized to construct piezoelectric transducer apparatuses of different characteristics. Further, transducer apparatuses

25   thus constructed have disengaged gain and phase characteristics.

Tables 1 and 2 below lists a few possible bases suitable for use in the construction of the effective surface electrodes for the sensor units that are attached to the body structure of the inventive piezoelectric transducer apparatuses. Note that these base listings are for second order systems complying

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to those described in the governing equation (7) and (8). Table 1 lists bases for those constructions in which waves are in the $x > 0$ direction. Table 2 lists bases for $x < 0$. In the Tables, bases are lists in the left column. Right columns of both Tables outlines transfer function induced by the system adopting the corresponding base.

Table 1

Base in Spatial Filters, $x > 0$

Base in System	Transfer Function Induced by the System
$e^{\alpha x}$	$\dfrac{1}{s - \alpha}$
$e^{-\alpha x}$	$\dfrac{1}{s + \alpha}$
$e^{j\alpha x}$	$\dfrac{1}{s - j\alpha}$
$e^{-j\alpha x}$	$\dfrac{1}{s + j\alpha}$
$e^{\alpha x} \, e^{j\alpha x}$	$\dfrac{1}{s - (\alpha + j\alpha)}$
$e^{-\alpha x} \, e^{-j\alpha x}$	$\dfrac{1}{s + (\alpha + j\alpha)}$
$e^{j\alpha x} - e^{-j\alpha x}$	$\dfrac{2i}{s^2 + \alpha^2}$
$e^{j\alpha x} + e^{-j\alpha x}$	$\dfrac{2s}{s^2 + \alpha^2}$
$\sin(\alpha x)$	$\dfrac{\alpha}{s^2 + \alpha^2}$
$\cos(\alpha x)$	$\dfrac{s}{s^2 + \alpha^2}$

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$\sinh(\alpha x)$	$\dfrac{\alpha}{s^2 - \alpha^2}$
$\cosh(\alpha x)$	$\dfrac{s}{s^2 - \alpha^2}$
$e^{-\alpha x}\sin(\beta x)$	$\dfrac{\beta}{(s+\alpha)^2 + \beta^2}$
$e^{-\alpha x}\cos(\beta x)$	$\dfrac{(s+\alpha)}{(s+\alpha)^2 + \beta^2}$
$x^n e^{\alpha x}$	$\dfrac{n!}{(s-\alpha)^{n+1}}$
$e^{-\alpha x}\sinh(\beta x)$	$\dfrac{\beta}{((\alpha+s)-\beta)((\alpha+s)+\beta)}$
$e^{-\alpha x}\cosh(\beta x)$	$\dfrac{\alpha+s}{((\alpha+s)-\beta)((\alpha+s)+\beta)}$

Table 2

Base in Spatial Filters, $x < 0$

Base in System	Transfer Function Induced by the System
$e^{\alpha x}$	$\dfrac{1}{\alpha - s}$
$e^{-\alpha x}$	$-\dfrac{1}{\alpha + s}$
$e^{j\alpha x}$	$\dfrac{1}{j\alpha - s}$
$e^{-j\alpha x}$	$-\dfrac{1}{j\alpha + s}$

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$e^{\alpha x} \quad e^{j\alpha x}$	$\dfrac{1}{(\alpha + j\alpha) - s}$
$e^{-\alpha x} \quad e^{-j\alpha x}$	$\dfrac{1}{(\alpha + j\alpha) + s}$
$e^{j\alpha x} - e^{-j\alpha x}$	$-\dfrac{2i\alpha}{s^2 + \alpha^2}$
$e^{j\alpha x} + e^{-j\alpha x}$	$-\dfrac{2s}{s^2 + \alpha^2}$
$\sin(\alpha x)$	$-\dfrac{\alpha}{s^2 + \alpha^2}$
$\cos(\alpha x)$	$-\dfrac{s}{s^2 + \alpha^2}$
$\sinh(\alpha x)$	$-\dfrac{\alpha}{s^2 - \alpha^2}$
$\cosh(\alpha x)$	$-\dfrac{s}{s^2 - \alpha^2}$
$e^{-\alpha x} \sin(\beta x)$	$-\dfrac{\beta}{(\alpha + s)^2 + \beta^2}$
$e^{-\alpha x} \cos(\beta x)$	$-\dfrac{(\alpha + s)}{(\alpha + s)^2 + \beta^2}$
$|x|^n e^{\alpha x}$	$\dfrac{n!}{(s + \alpha)^{n+1}}$
$e^{-\alpha x} \sinh(\beta x)$	$-\dfrac{\beta}{((\alpha + s) - \beta)((\alpha + s) + \beta)}$
$e^{-\alpha x} \cosh(\beta x)$	$-\dfrac{\alpha + s}{((\alpha + s) - \beta)((\alpha + s) + \beta)}$

If the body structure of a piezoelectric construction is mathematically divided into left ($x < 0$) and right ($x > 0$) sections with respect to the target of origin selected for the system, then, as Tables 1 and 2 clearly shows, the Laplace

5 transform applied to the left and right sections of the body structure in fact induced

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transfer functions that cancel each other. This is because that the transfer functions for the two sections have the same amplitude but are out of phase spontaneously. Specifically, if the instantaneous phase in a system at one side of its targeted origin (x > 0) is a, then the corresponding phase at the opposite side (x

5   < 0) is automatically $-a$. Spatial filters in accordance with the present invention thus do not really escape the rules of a causal system but, in fact, resulting into signals into the opposite directions with respect to the target origin with reversed phases. This is the cause for the desirable characteristics of the piezoelectric transducer apparatus of the present invention that the phase characteristics is

10 totally disengaged from the status of the gain.

Piezoelectric transducer apparatus according to the present invention also exhibits a characteristics of superposition. Spatial filters can be constructed by linear superposition in the spatial domain. In other words, the surface electrode of the sensor unit of a piezoelectric construction can be designed to be the

15 superposition of more than one known spatial filter functions, whose functional characteristics are known. The only issue to concern is that the superposition result of all these candidate functions needs to be able to be defined in the infinite domain.

Based on the above, different band-pass filters can be constructed utilizing the

20 piezoelectric transducer apparatus of the present invention. Figure 12 shows the gain characteristics as a function of frequency for a band-pass filter constructed by the superposition of discrete spatial filters. The band-pass filter built utilizing the concept of functional superposition may thus enjoy an expanded filtering band than the discrete filters. This effectively broadens the pass band, as is illustrated in

25 Figure 13A.

Figures 13A and 13B respectively show the gain and phase characteristics as functions of frequency for a band-pass filter that exhibit increased effective frequency range. Reference numerals 134, 135 and 136 in Figure 13A represent the useful bandwidth achieved by the original system 131, achieved after the first-

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order filtering 132, and after the second-order filtering 133 respectively. The substantially constant phase value represented by curve 137 in Figure 13B indicates the fact that the superposition to construct a band-pass filter does not alter the phase characteristics of the system.

5   Superpositioning assists in simplifying the manufacture of piezoelectric apparatuses. Figure 14 schematically illustrates the superposition of discrete spatial filters involving no change in the direction of polarization for the design of the inventive piezoelectric transducer apparatus. The drawing schematically illustrates the superposition of the gain characteristics 141 of a first filter having

10   the exponential bases e^{jkx} and e^{-jkx} and the gain 142 of a second filter with the exponential base $e^{-k|x|}$. The drawing schematically shows that the gains 141 and 142 are superpositioned into the resultant gain 143. The superpositioned gain 143 becomes an all-positive gain characteristics within the entire frequency range. This effectively simplifies the fabrication of the piezoelectric device as only a

15   positive electrode is needed. It becomes unnecessary to prepare positive and negative electrodes, electrode of reversed polarization profiles, over the same surface of the piezoelectric workpiece. Fabrication cost for such piezoelectric devices becomes optimized.

In the design concept based on the theory of wave propagation, spatial filter

20   with target origin set to the free end has an even function characteristics. If the target origin is set to the fixed end, the characteristics is an odd function. Thus, if the surface electrode of a piezoelectric construction contains trigonometric base of either the sine or cosine function, it is possible to automatically expand into a complete sine or cosine function in the infinite domain. This can be achieved if

25   the cosine characteristics in the case of free-end target origin is an even function, and the sine characteristics in the case of fixed-end target origin is an odd function.

Figures 15A and 15B schematically illustrate the use of the method of image in the expansion of a sine function onto the infinite domain in the design of an inventive piezoelectric transducer apparatus based on a fixe-free cylindrical body

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structure. In Figure 15A, a piezoelectric construction based on a fixed-free body structure is schematically illustrated. The sine base of its electrode schematically represented by reference numeral 151 has the finite 1/4 of a full sinusoidal cycle that can be transferred into the infinite domain by employing the imaging principle, combined with the arrangement that one end of the elongated body structure set as the fixed end 30 and the other as the free end 40. This is reflected in Figure 15B in which the domain is infinite.

Figures 16 and 17 illustrate two other similar designs. Figures 16A and 16B schematically illustrate the use of the method of imaging in the expansion of a sine function onto the infinite domain in the design of an inventive piezoelectric transducer apparatus based on a free-free cylindrical body structure. Figures 17A and 17B schematically illustrate the use of the method of imaging in the expansion of a sine function onto the infinite domain in the design of an inventive piezoelectric transducer apparatus based on a fixed-fixed cylindrical body structure.

In addition to the low-pass filters made from the inventive piezoelectric transducer apparatus as described above, it is possible to implement high-pass, band-pass, band-reject and other types of filters. Except for the above-described methodologies, the construction of these filters require other additional design considerations including, for example, the integration of certain sensor interfacing circuits.

Figure 18 is a perspective view illustrating an embodiment of a spatial filter based on the inventive piezoelectric sensor apparatus having a fixed-free cylindrical body structure. In this piezoelectric construction, surface electrode 181 of a sensor unit attached to the body structure, which functions as a spatial filter, sets its target origin at the fixed end 30 of the system. Within the same construction, another surface electrode 182 of another sensor unit also adhered to the body structure and functions as another spatial filter sets its target origin at the free end 40 of the same system. Signals from both electrodes 181 and 182 can be

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picked up and summed up together in order to directly provide a zero in the entire system. Relative gain factors of both systems (of electrodes 181 and 182 respectively) can be adjusted by controlling the operation of the gain circuit 183, or by tailoring the shape and size of the surface electrodes themselves. As a result,

5   a band-pass filter construction exhibiting the gain characteristics such as described in Figures 19A and 19B can be built

Figures 19A and 19B respectively show the gain and phase characteristics as functions of frequency for an embodiment of a band-pass filter based on the inventive piezoelectric sensor apparatus having a fixed-free cylindrical body

10   structure as described in Figure 18. Gain characteristics 191 in Figure 19A demonstrates the functionality of a band-pass filter. The phase characteristics 192 in Figure 19B indicates that the phase remains virtually fixed regardless of the alteration of the gain within the same frequency range.

For the construction of a high-pass filter, the one illustrated in Figure 20 for

15   example, a piezoelectric construction similar to that of Figure 18 is used. The difference rests in the fact that the interface circuit is integrated differently. The signal picked up at the fixed end 30 of the body structure via the electrode 201 is fed to a current amplifier. The first filter is one setting its target origin at the fixed end 30 of the body structure. A charge amplifier 205 is connected to the electrode

20   202 for the spatial filter setting its target origin at the free end 40 of the body structure. Relative gains for the first and second embedded filters are summed up, and the resultant signal as summed up exhibits the characteristics of a high-pass filter such the one depicted in Figures 21A and 21B.

The above-described embodiments of the constructions for the inventive

25   piezoelectric transducer apparatus employed designs that set their target origins at the symmetrical center location and the boundary locations that provide substantial symmetry for the entire construction. This arrangement secures symmetry of the effective surface electrodes separated by the target origin. This is an advantageous practice for flexible control of the characteristics of the filter thus constructed.

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However, in case that the target origin is not set for symmetry, the section corresponding to the asymmetric portion of the system has to be added back. Stated alternatively, the missing sections less the symmetry of the system are returned back to the system by patching the corresponding electrode surface areas back to the body structure. This effectively brings the lost signal (not picked up by the electrode) back into the system, so that the physical finite domain can be transferred into the mathematical infinite domain.

Figure 22 is a perspective view illustrating the electrode design of an asymmetric effective surface having a target origin that is neither located at the body structural center nor at the body structural boundary. In the depicted example of Figure 22, the target origin 1 is closer to the fixed end 30 of the body structure. Without the symmetry, wave propagation model can not be complete for the desired device functional characteristics. For the asymmetric selection of the target origin at the location closer to the free end of the body structure such as illustrated in Figure 23, the missing section of the electrode at the free end can be patched back to the body structure so that the signal picked up becomes complete. Figure 24 shows such a patched system.

Figure 24 is a perspective view illustrating the asymmetric effective surface electrode of an embodiment of the inventive piezoelectric transducer apparatus designed by the superposition of discrete effective surface electrodes, with the fixed-free cylindrical body structure. In the drawing, 241 represents a complete electrode for a first filter embedded in the system, and 242 represents a patched one.

Figures 25 and 26 respectively illustrate alternate electrode patching designs for the asymmetric system of Figure 23 as compared to the patching of Figures 24. Specifically, Figure 25 is a perspective view illustrating another asymmetric effective surface electrode of an embodiment of the inventive piezoelectric transducer apparatus designed by the superposition of discrete effective surface electrodes, with the target origin biased toward the free end of the fixed-free

cylindrical body structure. Figure 26 is a perspective view illustrating yet another asymmetric effective surface electrode of an embodiment of the inventive piezoelectric transducer apparatus designed by the superposition of discrete effective surface electrodes, with the target origin biased toward the free end of the fixed-free cylindrical body structure.

In the case of Figure 25, the missing section 252 of the electrode at the free end is placed back to the body structure. By contrast, in Figure 26, the place back of the missing section of the electrode is different.

For patching of the surface electrode at the fixed end of the body structure, such as for the construction of Figure 22, the implementation is different from that described in Figures 25 and 26. Since wave propagation at the fixed end of the body structure exhibits an odd function, therefore the patching for the missing section of the electrode must be subtractive. Figures 27 - 30 respectively illustrate how this can be implemented in various ways. In comparison, the patching in the case of Figure 25 and 26 are additive, as are label in the drawings by the same polarity signs of "+" as the main electrode section of those constructions.

Specifically, Figure 27 is a perspective view illustrating the asymmetric effective surface electrode of an embodiment of the inventive piezoelectric transducer apparatus designed by the superposition of discrete effective surface electrodes, with the target origin biased toward the fixed end of the fixed-free cylindrical body structure.

The perspective view of Figure 28 illustrates another asymmetric effective surface electrode of an embodiment of the inventive piezoelectric transducer apparatus designed by the superposition of discrete effective surface electrodes, with the target origin biased toward the fixed end of the fixed-free cylindrical body structure.

Figure 29 is a perspective view illustrating yet another asymmetric effective surface electrode of an embodiment of the inventive piezoelectric transducer apparatus designed by the superposition of discrete effective surface electrodes,

with the target origin biased toward the fixed end of the fixed-free cylindrical body structure.

Figure 30 is a perspective view illustrating still another asymmetric effective surface electrode of an embodiment of the inventive piezoelectric transducer apparatus designed by the superposition of discrete effective surface electrodes, with the target origin biased toward the fixed end of the fixed-free cylindrical body structure.

In certain situations in which boundary condition at one or both boundaries of the body structure of a piezoelectric construction includes factors such as damping or spring elasticity substantially different from those discussed above in the fixed-free elongated body structure, design considerations become different. In these constructions, wave propagation reaching to these boundaries behaves differently as both the phase and amplitude of the reflected wave become substantially altered with respect to those simple fixed-free structures discussed above. To resolve this discrepancy, off-set weight has to be added to the system. Figure 31 illustrates such a weighted system. Figure 31 is a perspective view illustrating an embodiment of the inventive piezoelectric sensor apparatus having the boundary condition set neither to the fixed nor to the free end.

For piezoelectric constructions such as that of Figure 31, interface circuits can be incorporated and integrated into the system in order to eliminate the adverse effects placed on the system by the weighting at the body structure boundary. Figure 32 outlines such an interface circuit-augmented construction. Figure 32 is a schematic diagram illustrating the application of an embodiment of the inventive piezoelectric transducer apparatus in an inspection and test device by integrating with an interface circuit and featuring a suitably-selected effective surface electrode.

In the drawing, a charge amplifier 323 is connected to the incomplete spatial filter surface electrode 326. Another charge amplifier 322 is connected to the patched electrode 327, and a current amplifier 321 is, in turn, connected to another

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patched electrode 328 of the reversed electrode polarity. Gains of current amplifier 321 and of charge amplifier 322 are further augmented by gain adjustment circuits 325 and 324 respectively. With this arrangement, the wave propagation in the entire system can still be transferred into the infinite domain.

5   Figure 33 illustrates the characteristics of the device of Figure 32 in the complex plane.

Piezoelectric transducer apparatus in accordance with the present invention can also be utilized in the construction of active point sensor devices. Based on the mutually reciprocating phenomenon of piezoelectricity and electrostriction,

10   piezoelectric constructions of the present invention functioning as sensors and actuators can be integrated with electronic controllers and compensators for the construction of active feedback examination systems.

Figure 34 is a block diagram illustrating the basic circuit configuration of a sense and control device having an active sensor feedback loop based on either the

15   expansion or the compression effect of the sensor body structure. The active sensor system 349 outlined in Figure 34 comprises a piezoelectric sensor construction 348 in the form of the piezoelectric transducer apparatus of the present invention. At least one sensor units 341 is attached to the body structure 343 of the piezoelectric construction 348. At least one actuator unit 342 is

20   similarly attached to the body structure 343.

The active sense and control system 349 of Figure 34 further comprises an interface circuit 344 for the sensor unit 341 and another interface circuit 346 for the actuator unit 342. A compensator circuit 345 is also installed in the system that provides feedback compensation to the electronics of the system in order to

25   make up an active sense and control system, 349. A target structure 347 can be received by the piezoelectric construction 348 so as to be inspected and/or controlled.

Figure 35 is a block diagram illustrating the basic circuit configuration of another sense and control device having an active sensor feedback loop based on

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torsional effect of the sensor body structure. The system of Figure 35 is similar to that of Figure 34 except that the system is utilized for sense and control of torsional vibrations in the target structure 347. Both systems of Figure 34 and 35 features disengaged gain and phase characteristics since the piezoelectric

5   construction employed in their respective system are constructed in accordance with the disclosure of the present invention.

In the system of Figure 34, as the inspected structure 347 receives vibration, sensor unit 341 of the sensor construction 348 picks up the vibration and generates the corresponding electric signal. The picked up signal is processed in the

10   interface circuit 344 and the output $q(t)$ also fed to the compensator 345 for feedback into the piezoelectric sensor construction 348. This can implemented as the output $q(t)$ fetched to the compensator 345 is processed and the resulting compensation signal sent to the interface circuit 346 for feedback into the piezoelectric construction 348. Actuator unit 342 connected to interface circuit

15   346 is responsible for the fetch of the feedback into the construction. Such a close-loop feedback circuit configuration is thus able to implement active piezoelectric sensing.

Operation in the system of Figure 35 is without substantial discrepancy when compared to the system of Figure 34, except that the system of Figure 34 is

20   suitable for inspecting longitudinal vibrations while the system of Figure 35 suitable for torsional vibrations.

Piezoelectric systems illustrated in Figures 34 and 35 are constructed in accordance with the teaching of the present invention. They are different from those conventional system in that the phase characteristics is totally decoupled

25   from the gain of the system. Figure 36 illustrates the characteristics curve of these active systems in the infinite domain.

While the above is a full description of the specific embodiments, various modifications, alternative constructions and equivalents may be used. For example, although piezoelectric transducer apparatuses with sensor constructions

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having the body structure in the form of elongated rods complying to second order systems are utilized as examples for the mathematical development of the underlying principle of the present invention, use of body structures of other physical dimensions are possible. Further, piezoelectric transducer apparatuses mathematically other than a second order system shape should not be considered as not being encompassed in the scope of the present invention. Therefore, the above description and illustrations should not be taken as limiting the scope of the present invention which is defined by the appended claims.